GCE Examinations Advanced Subsidiary / Advanced Level

Statistics Module S3

Paper A

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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S3 Paper A - Marking Guide

1. (a)
$$\hat{\mu} = \overline{V} = \frac{1439}{10} = 143.9$$

(b)
$$\overline{V} \pm 1.96 \frac{\sigma}{\sqrt{n}} = 143.9 \pm 1.96. \frac{\sqrt{130}}{\sqrt{10}}$$
 M1 A1

M1 A1

A1

3. (a) let
$$F = \text{time on French and } E = \text{time on English}$$

let $A = F + E$: $A \sim N(55 + 90, 10^2 + 18^2) = N(145, 424)$ M1 A1
 $P(A > 120) = P(Z > \frac{120 - 145}{\sqrt{424}})$ M1
 $= P(Z > 1.21) = 0.8869$ M1 A1

(b)
$$P(E > 2F) = P(E - 2F > 0)$$
 M1
let $B = E - 2F$ $\therefore B \sim N(90 - 2 \times 55, 18^2 + 4 \times 10^2) = \sim N(^20, 724)$ M1 A1
 $P(B > 0) = P(Z > \frac{0 + 20}{\sqrt{724}})$ M1
 $= P(Z > 0.74) = 1 - 0.7704 = 0.2296$ M1 A1 (11)

4. expected freq. males/watched =
$$\frac{36 \times 40}{80}$$
 = 18

$$males/stranded = \frac{16\times40}{80} = 8$$
 M1 A2

 H_0 : no difference in preference of males and females H_1 : difference in preference of males and females B1

2.143 < 4.605 : not significant

there is no evidence of a difference in preference of males and females A1 (11)

5.	(a)			
3.	(a)	temp. 16 9 11 5 7 21 12 15		
		position 2 15 5 19 10 4 6 11		
		temp. rank 2 6 5 8 7 1 4 3		
		temp. rank 2 6 5 8 7 1 4 3 pos'n rank 1 7 3 8 5 2 4 6 d^2 1 1 4 0 4 1 0 9		
			1.62.42	
		$\sum d^2 = 20$ $r_s = 1 - \frac{6 \times 20}{8 \times 63} = 0.7619$	M2 A2 M1 A1	
		$r_s - 1 - \frac{1}{8 \times 63} = 0.7019$	WH AI	
	<i>(b)</i>	$H_0: \rho = 0 H_1: \rho > 0$	B1	
		$n = 8, 5\%$ level : C.R. is $r_s > 0.6429$	M1 A1	
		0.7619 > 0.6429 ∴ significant there is evidence that she will do better at higher temperatures	A1	
	(-)			
	(c)	e.g. this would not answer her query which relates to how well she does compared to others, all runners may be slower in higher temps	B2	(12)
6.	(a)	let $W =$ weight of component $\therefore W \sim N(46.7, 1.8)$		
	()	$\overline{W} \sim N(46.7, \frac{1.8}{12}) = \sim N(46.7, 0.15)$	M1 A1	
		47. 467.		
	<i>(b)</i>	$P(\overline{W} > 47) = P(Z > \frac{47 - 46.7}{\sqrt{0.15}})$	M1	
		= P(Z > 0.77) = 1 - 0.7794 = 0.2206	M1 A1	
	(c)	$H_0: \mu = 46.7 H_1: \mu \neq 46.7$	B1	
	, ,	5% level :: C.R. is $z < 1.96$ or $z > 1.96$	B1	
		test statistic = $\frac{46.5-46.7}{\sqrt{\frac{1.8}{120}}}$ = -0.816	M2 A2	
		not in C.R. do not reject H ₀		
		not in C.R. do not reject 110		
		no evidence of change in mean weight	A1	(12)
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7.	(a)	no evidence of change in mean weight H_0 : B(16, 0.1) is a suitable model		(12)
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Total (75)

Performance Record – S3 Paper A

Question no.	1	2	3	4	5	6	7	Total
Topic(s)	confidence interval	sampling	linear comb. of Normal r.v.	conting. table	Spearman's, hyp. test	dist. of sample mean, hyp. test	goodness of fit, binomial	
Marks	6	7	11	11	12	12	16	75
Student								
	<u> </u>							