GCE Examinations Advanced Subsidiary / Advanced Level

Statistics Module S3

Paper C

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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S3 Paper C - Marking Guide

2. (a)
$$\overline{T} \sim N(28.5, \frac{7.2^2}{8}) = \sim N(28.5, 6.48)$$
 M1 A1

(b)
$$P(25 < \overline{T} < 30) = P(\frac{25 - 28.5}{\sqrt{6.48}} < Z < \frac{30 - 28.5}{\sqrt{6.48}})$$
 M1 A1
= $P(-1.37 < Z < 0.59) = 0.7224 - (1 - 0.9147) = 0.637$ M1 A1 (6)

3. (a)
$$E(X) = (2 \times 0.05) + (4 \times 0.15) + (7 \times 0.3) + (k \times 0.5)$$
 M1
= 2.8 + 0.5k A1

(b)
$$E(2\overline{X} - 5) = 2(2.8 + 0.5k) - 5 = k + 0.6$$
 M1
 $\therefore \text{ bias} = 0.6$ M1 A1

(c) unbiased est. of
$$k = 2\overline{X} - 5.6 = (2 \times 8.34) - 5.6 = 11.08$$
 M1 A1 (7)

4. let
$$T = \text{total mass of waste}$$

$$T \sim N(8 \times 6.8 + 3 \times 3.2, 8 \times 1.5^{2} + 3 \times 0.6^{2}) = N(64, 19.08)$$

$$P(T > 70) = P(Z > \frac{70 - 64}{\sqrt{19.08}})$$

$$= P(Z > 1.37) = 1 - 0.9147 = 0.0853$$
M1 A1

(7)

5.
$$H_0: \mu_A = \mu_N$$
 $H_1: \mu_A < \mu_N$ B1
5% level :: C.R. is $z < ^-1.6449$ B1
test statistic = $\frac{32.8-35.1}{\sqrt{\frac{4.6^2}{50} + \frac{8.0^2}{190}}} = ^-2.6382$ M2 A2

in C.R.
$$\therefore$$
 reject H₀ M1
there is evidence that those in school teams complete task quicker A1 (8)

6. expected freq. Highfield/English =
$$\frac{80 \times 46}{120}$$
 = 30.67 M1 A1

 H_0 : no difference in proportions at the two schools H_1 : there is a difference in proportions at the two schools B1

O
 E

$$(O-E)$$
 $\frac{(O-E)^2}{E}$

 32
 30.67
 1.33
 0.0577

 14
 15.33
 $^{-1}$.33
 0.1154

 48
 49.33
 $^{-1}$.33
 0.0359

 26
 24.67
 1.33
 0.0717

$$\therefore \Sigma \frac{(O-E)^2}{E} = 0.2807$$
 M1 A2

$$v = 1, \chi^2_{\text{crit}}(10\%) = 2.705$$
 M1 A1

0.2807 < 2.705 : not significant

there is no evidence of a difference in proportions at the two schools A1 (11)

7. (a)
$$S_{pp} = 70932 - \frac{1176^3}{20} = 1783.2$$
 M1

 $S_n = 19213 - \frac{511^3}{20} = 6156.95$ M1

 $S_p = 27188 - \frac{11786-11}{20} = 2858.8$ M1

 $r = \frac{-2858}{\sqrt{183.0-96595}} = 70.8628$ M1 A1

(b) $H_0: p = 0$ $H_1: p < 0$ B1

 $n = 20, 1\%$ level : . C.R. is $r < 0.5155$ M1 A1

(c) $n = 20, 1\%$ level expected with lower rest pulse are fitter there is evidence that people with lower rest pulse are fitter there is evidence that people with lower rest pulse are fitter there is evidence that people with lower rest pulse are fitter e.g. it seems reasonable that the fitness of those with a given rest pulse should follow a normal dist, and vice versa

8. (a) e.g. particles are emitted singly, at random and at a constant rate (for near future given long half-life) so seems suitable

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8. (b) $\hat{\mu} = x = \sum_{j=1}^{j} \frac{96}{90} = 1.2$ M1 A1

$$\sum_{j=1}^{j} \frac{25}{2} = \frac{96}{20} = 1.2$$
 M1 A1

(c) variance = mean as would be expected with a Poisson distribution B1

(d) $H_0: Po(1.2)$ is a suitable model

 $H_1: Po(1.2)$ is not a suitable model

 $P(0) = l^{1/2} = 0.3012$
 $P(1) = 1.2e^{-1/2} = 0.0867$ M1 A2

 $P(4) = \frac{112e^{-1/2}}{\sqrt{2}} = 0.0867$ M1 A2

 $P(4) = \frac{112e^{-1/2}}{\sqrt{2}} = 0.0260$

× 80 to give exp. freqs then freq of $\geq 5 = (80 - \text{sum of others})$

∴ exp. freqs are 24.10, 28.91, 17.35, 6.94, 2.08, 0.62 M1 A1

combining groups ≥ 3 M1

 $O = E = (O - E) = \frac{(O - E)^2}{E^2}$
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Total (75)

Performance Record – S3 Paper C

Question no.	1	2	3	4	5	6	7	8	Total
Topic(s)	sampling	dist. of sample mean	bias	linear comb. of Normal r.v.	diff. of means hyp. test	conting. table	pmcc, hyp. test	goodness of fit, Poisson	
Marks	5	6	7	7	8	11	11	20	75
Student									