

GCSE MATHEMATICS 8300/1F

Foundation Tier Paper 1 Non-Calculator

Mark scheme

November 2019

Version: 1.0 Final



Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
A	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Question	Answer	Mark	Comments
1	<u>9</u> 10	B1	
2	<i>x</i> = 2	B1	
3	$0.3 > \frac{1}{4}$	B1	
4	7	B1	

Question	Answer	Mark	Comments		
	Alternative method 1 – traditional	method			
-	304 or 1520 with the 0 correct for the multiplication by 20 or 144 or 1680 with the 0 correct for the multiplication by 70	M1	values may be seen separately or in rows if 1520 or 1680 incorrect, placeholder 0, or equivalent must be present		
-	their 304 + their 1520 or their 144 + their 1680 1824	M1dep A1			
_	Alternative method 2 – grid metho				
-	At least three of 1400, 280, 120 and 24	M1	may not be in a grid		
-	their 1400 + their 280 + their 120 + their 24	M1dep			
_	1824	A1			
5	Alternative method 3 – Napier's bones				
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1	oe at least three of the calculated values correct		
-	Attempt to total correctly four diagonals for their table with carrying figure seen	M1dep			
	1824	A1			
F	Alternative method 4 and Additional Guidance are on the next page				

	Alternative method 4 – breaking calculation down				
	Calculation broken down correctly with a maximum of one calculation error	M1	eg 76 × 10 × 2 (+) 70 × with at least two of 1520, correct	. ,	
	Addition of their parts	M1dep	eg 1520 + 280 + 24		
	1824	A1			
	Additional Guidance				
	70 × 20 + 6 × 4 (= 1424)			M0M0A0	
	Alt 1 304 + 152 = 456			M0M0A0	
E cont	Alt 1 If the 0 is missing, allow 0 to be replaced by x or a placeholder space (may be implied by their 4 in units column of their final answer)				
5 cont	Alt 3 Diagonal lines must slope cons	sistently fo	r M1 unless recovered		
	Alt 3 Diagonal lines missing is M0 unless recovered				
	Alt 3 For M1M1dep, a carrying figure must be seen or implied				
	Alt 3 Answer must be clearly stated				

Question	Answer	Mark	Comments	
6(a)	8	B1		
6(b)	16	B1		
	Physics and French	B1	either order mark intention eg accept P and F	
6(c)	Additional Guidance			
	Condone incorrect spelling			

	All six of the following criteria correct:		B1 any 5 of the criteria o	correct		
6(d)	 width of bar overall height of bar correct gap from previous bar bar split in half horizontally appropriate shading/labelling 'history' label correct and in correct place 	B2				
	Additional Guidance					
	Apply a generous interpretation to their attempt to shade					
	The shading for the boys needs to be darker than the shading for the girls (the part of the bar for the girls can be left unshaded)					
	Accept label(s) of 'boys' and/or 'girls' instead of shading					
	Ignore any numbers on bars, eg labelled 9 and 9					

7(a)	0.31	B1	oe eg .31	
	Additional Guidance			
	Final answer 31 (even if 0.31 seen in	working)		В0
				·

7(b)	0.08	B1	oe eg .08
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Question	Answer	Mark	Comme	nts
	8.6 and 0.4	B1	either order	
	9(.0)	B1ft	ft their two numbers SC1 answer 9(.0), cards	blank
	Ade	ditional G	uidance	
	Do not allow misreads of the card value	ues in this	question	
	8.6 and 0.27 Answer 8.87			B0B1ft
9(a)	8.6 and 6.3 Answer 14.9			B0B1ft
8(a)	0.27 and 6.3 Answer 6.57			B0B1ft
	0.27 and 0.4 Answer 0.67			B0B1ft
	6.3 and 0.4 Answer 6.7			B0B1ft
	8.6 + 0.27 = 8.87 Answer 9			B0B1ft
	(ignore rounding if correct decimal seen)			
	Cards take precedence, but if cards or answer line are blank, mark all other working and award the lowest mark unless their choice is unambiguously identified			

	8.6 and 0.27 in this order only	B1		
	8.33	B1ft	correct or ft their two nu	mbers
	Ade			
	Do not allow misreads of the cards in	this quest	ion	
8(b)	Examples of follow through (there are many)			B0B1ft
	0.27 and 8.6 Answer –8.33			
	6.3 and 0.4 Answer 5.9			
	Cards take precedence, but if cards or answer line are blank, mark all other working and award the lowest mark unless their choice is unambiguously identified			

Question	Answer	Mark	Comme	nts
	Correct indication of mistake	B1	eg (6.10) should be 7(.0 or 2 × 3.5(0) (= 7.(00)) or cost of pens is wrong	
	11.25 B1			
	Additional Guidance			
9	Accept any correct indication of mistake eg two lots of 50p don't equal 10p			
	Condone (£) 11.25 p for second B1			
	Any reference to cost of rulers (words or calculations) being incorrect cannot score first B1			
F	Response only references the decimal points not being lined up correctly			В0

Question	Answer	Mark	Comme	nts	
	(A =) 2000 000 and (B =) 500 000 and (C =) 400 000 and smallest answer C B largest answer A	B3	allow values or calculation letters on answer lines B2 two of (A =) 200000 (B =) 500000, (C = B1 (A =) 2000000 or (or (C =) 400000	00,) 400 000	
-		ditional G			
-	Answer line takes precedence over v				
	Any of the original value(s) misread of calculations				
	Once a correct evaluation has been s manipulate it for up to B2				
	eg 400,000 = 0.004 million, 0.5 millio	B2			
10	Accept values in words eg accept ha				
	Ordering of their values is irrelevant when awarding B2 or B1				
	Ignore (incorrect) spacings or any us continental notation	e of comm	as within numbers or		
	eg 4 00000			B3	
	50 0000				
	2,00000,0 eg 40.0000				
	500.000			B3	
	2.000.000				
	С				
	В			B0	
	A				
	no correct calculations seen				

Question	Answer	Mark	Comment	ts
-	0 B1 oe fraction, decimal or pe			rcentage
-	zero or nought			B1
	0%			B1
	$\frac{0}{n}$; <i>n</i> is an integer > 0, eg $\frac{0}{200}$		B1	
-	With B1 scored, ignore probability wo	s contradictory		
	eg 0, impossible			B1
	eg 0, unlikely			B0
11(a)	Zero chance	B0		
11(0)	Nothing or nil			B0
	0 out of 200			B0
	0 in 200			B0
	No			B0
	No chance		B0	
	Impossible			B0
	Not possible			B0
	Any of the B0 responses above, with	a B1 ansv	ver	B1
	0 : 200 or 0 to 200 (even with B1 re	sponse, s	still scores B0)	B0

Question	Answer	Mark	Comme	nts	
	200 - 79 - 90 or 31 or $\frac{79}{200} + \frac{90}{200}$ or $1 - \left(\frac{79}{200} + \frac{90}{200}\right)$ or $\frac{(200 - 79 - 90)}{200}$ or $\frac{169}{200}$	M1	oe eg 200 – (79 + 90) eg 0.395 + 0.45 or 0.84 accept 0.16 or 16% if no		
	31 or 0.155 or 15.5% A1 accept 0.10 of 10 % if 1 Additional Guidance Additional Guidance				
11(b)	Ignore incorrect cancelling or incorrect percentage or incorrect rounding after				
	eg $\frac{31}{200}$ seen, then answer $\frac{3}{20}$			M1A1	
-	eg 15.5% seen, then answer 15%			M1A1	
-	Answer 0.16 or 16% with M1 work no	t seen		M1A1	
	31 : 200 or 31 : 169 or 31 out of 20	n 200	M1A0		
	Ignore probability words unless contra				
	eg $\frac{31}{200}$ unlikely			M1A1	
	eg $\frac{31}{200}$ likely			M1A0	

Question	Answer	Mark	Comments		
	Alternative method 1				
	x + x + 19 = 105 or $\frac{105 - 19}{2}$ or $\frac{86}{2}$ or 43	M1	oe equation any letter may be implied by second mark		
-	$\frac{105-19}{2}$ + 19 or 62	M1dep	oe 62 seen is M2 (unless clearly from incorrect working)		
-	62 or 0.59(0) or 59.(0)%	A1	oe SC2 $\frac{43}{105}$ or 0.41 or 41% or better		
-	Alternative method 2	1 1			
-	<i>y</i> + <i>y</i> – 19 = 105	M1	oe equation any letter may be implied by second mark		
12	$\frac{105+19}{2}$ or $\frac{124}{2}$ or 62	M1dep	62 seen is M2 (unless clearly from incorrect working)		
	62 or 0.59(0) or 59.(0)%	A1	oe SC2 $\frac{43}{105}$ or 0.41 or 41% or better		
-	Alternative method 3				
	$\frac{105}{2}$ and $\frac{19}{2}$ or 52.5 and 9.5	M1			
	their 52.5 + their 9.5 or 105 – (their 52.5 – their 9.5) or 62	M1dep	62 seen is M2 (unless clearly from incorrect working)		
	62 105 or 0.59(0) or 59.(0)%	A1	oe SC2 $\frac{43}{105}$ or 0.41 or 41% or better		
-	Additional Guidance is on the next	page			

	Additional Guidance	
	Ignore any attempts to simplify or convert a correct fraction	
	Trial and Improvement leading to 62 (may go on to score full marks)	at least M1M1
Q12 cont	Trial and Improvement not leading to 62 or the correct answer	M0M0A0
	$\frac{19}{105}$ or $\frac{86}{105}$	M0M0A0
	62 : 105 or 62 : 43 or 62% or 62 out of 105	M1M1A0

Question	Answer	Mark	Comme	Comments	
13	(262 rounded to) 260 or (19.8 rounded to) 20 or 26 ÷ 2 13	M1 A1			
	Additional Guidance				
-	13 embedded eg 260 ÷ 13 = 20			M1A0	
-	Beware, 13 may not get full marks eg 262 ÷ 20 = 13.1, answer 13			M1A0	
	300 ÷ 20			M1A0	

Question	Answer	Mark	Comme	nts
	10 + 2 + 10 + 2 or 24 or 10 + 6 + 10 + 6 or 32	M1	oe may be seen in a ratio	
	10 + 2 + 10 + 2 or 24 and 10 + 6 + 10 + 6 or 32	A1	oe may be seen in a ratio	
-	3 : 4	B1ft	ft correct and full simplifi unsimplified ratio except with M1A1 scored SC2 6 : 7 SC1 12 : 14	
-	Ade			
-	Ignore any units given			
	Answer 3 : 4 with no incorrect working			M1A1B1
14	1:1.3	M1A1B0		
	Working with half perimeter consistently 12 : 16 = 3 : 4 answer 12 : 16 or 6 : 8 24 and 32 then 32 : 24 = 4 : 3 cannot be awarded B1ft as this would be			M1A1B1 M1A1B0 M1A1B0
-	full marks for an incorrect final answer 32 : 24			M1A1B0
-	24 : 42 = 4 : 7			M1A0B1ft
-	10:6=5:3			M0A0B1ft
-	20 : 12 = 10 : 6 (not fully simplified)			M0A0B0ft
-	20 : 60 = 1 : 3			M0A0B1ft
	14 : 22 = 6 : 10 = 3 : 5 (6 : 10 is an error, then simplifying this to 3 : 5 is not B1ft)			M0A0B0ft

Question	Answer	Mark	Comme	nts		
	Alternative method 1					
	5:1 or 1:5		may be implied by secor	nd mark		
	or $\frac{5}{6}$ or $\frac{1}{6}$ or 6 (parts)	M1	may be seen on diagram	1		
	180 ÷ 6 or 30	M1dep				
	150	A1				
	Alternative method 2					
15	5x + x = 180 or $6x = 180$	M1	any letter may be implied by secor	nd mark		
	180 ÷ 6 or 30	M1dep				
	150	A1				
	Additional Guidance					
	If Trial and Improvement used, 3 the answer for M2A1	80 seen is M2 bu	it 150 must be chosen as			
	360 ÷ 6			M1M0A0		

16	125	B1	

Question	Answer	Mark	Comments	
	Any two of (–1, –4), (0, –1), (1, 2), (2, 5) and (3, 8) or other correct points	M1	may be seen in a table may be implied by points plotted	
	At least two correct points plotted correctly or at least two of their points plotted correctly	M1	implied by correct line which does not have to extend from (-1, -4) to (3, 8) $\pm \frac{1}{2}$ small square	
17	Straight, ruled line from (–1, –4) to (3, 8)	A1	$\pm \frac{1}{2}$ small square ignore line beyond (-1, -4) and (3, 8)	
	Ad	Buidance		
	Ignore extra points listed or plotted			
	M marks can be scored even if wrong	/n		
	M marks are independent, the secon plotting of two of their points	n be awarded for correct		

	$\frac{3}{5}$		B1	$\frac{18}{30}$ or $\frac{9}{15}$ or	<u>6</u> 10
		B2		or 0.6(0) or 60%	6
18(a)			SC1	2 5	
	Ade	ditional G	Buidanc	e	
	$\frac{18}{30}$ or $\frac{9}{15}$ or $\frac{6}{10}$ followed by incorre	ct simplifi	cation o	r any conversion	B1

Question	Answer	Mark	Comments	
	$\frac{64}{100}$ × (30 + 20)	M1	oe eg 0.64 \times 50 or 64 \div 2 build up method must be complete	
	32	A1		
-	14 (out of 20)	A1ft	ft their 32 – 18 with M1A0 scored their 32 must be greater than 18 SC1 12.8 (or 13 after 12.8 is seen)	
	Ad	ditional G	uidance	
-	$\frac{14}{20}$ or 70%		M1A1A0	
	14 = 70% on answer line		M1A1A1	
F	Answer 32 or $\frac{32}{50}$	M1A1A0		
	$64\% \times 50$ with no further work	МО		
18(b)	$\frac{64}{100} \times 50 = 30$	M1A0A1ft		
	Answer 12Example of complete build-up (for 64% of 50) $10\% = 5$ (no working but correct) $6 \times 5 = 30$ (correct with working) $1\% = 0.5$ (no working but correct) $4 \times 0.5 = 0.20$ (incorrect but working shown so still on for M1) $= 30.20$ (implied correct addition)then $30.20 - 18 = 12.20$ Answer 12.20 (condone decimal value for ft)			
	Example of incomplete build-up (for 50% = 25 (no working but correct) 10% = 5 (no working but correct) 2% = 2 (incorrect and no working sh 	M0A0A0		

Question	Answer	Mark	Comments		
	Valid reason	B1	eg there might be 20 sh or the number of sheep con multiple of 10 or the ratio may have been or the numbers in the ratio be the actual numbers	uld be any simplified	
	Ade				
	Ignore irrelevant statements but do no				
	It doesn't mean 10 sheep it's just thei	r ratio		B1	
19(a)	The total number of animals is unkno	wn		B1	
	Could be 50 sheep			B1	
	Could be 20 : 6			B1	
	There are 10 sheep for every 3 cows number (of sheep/cows or total)	we just do	on't know the exact	B1	
	Could be 50 sheep and 18 cows (err	or seen)		B0	
	Could be 50 : 15 = 10 : 3 = 2 : 1 (e	error seen))	B0	
	It's only a ratio	B0			
	There are 10 sheep for every 3 cows		B0		
	There could be more than 10 sheep a	and more t	han 3 cows	В0	
	There might be more than 10 sheep /	might be	more than 3 cows	B0	

Question	Answer	Mark	Comme	nts
	Yes and valid working	B1	eg Yes and $(4 \times 3 =) 12$ or Yes and 4×3 is less that or Yes and $(13 \div 4 =) 3.25$ or Yes and $13 \div 4$ is more or Yes and $(13 \div 3 =) 4.3$ or Yes and $13 \div 3$ is more	an 13 oe oe than 3 oe . oe
19(b)	Ad	ditional G	Guidance	
	'No' or 'Cannot tell' ticked			B0
	Ignore irrelevant statements but do n	ot ignore o	contradictory statements	
	Allow correct reference to remainders	s or shortfa	alls in working	
	eg Yes and $13 \div 4 = 3$ with one (goa	t) left over		B1
	eg Yes and 13 ÷ 4 = 3 r1			B1
	eg Yes and 13 ÷ 4 = 3.1			B0
	Any evaluation must be fully correct of shortfall	or referenc	ce a remainder or	
	eg Yes and 13 ÷ 4 = 3.2			B0
	Any comparative statement must be eg Yes and $13 \div 4$ is less than 3	true		B0

Question	Answer	Mark	Comments
20	 The number rolled is even The number rolled is greater than 1 The number rolled is less than 5 The number rolled is prime 	B1	

	Ad	ditional G	or $bx = 3$ or $bx = -3$	M1A1A0
21	0.5 or $\frac{1}{2}$	A1ft	oe eg $\frac{3}{6}$ ft any equation of form 6x = a or $-6x = a$	
	6x = 3 or $-6x = -3$	A1	oe implied by correct answe	r
	$\pm 6x \text{ or } \pm 3$ or $8x - 2x = 10 - 7$ or $7 - 10 = 2x - 8x$	M1	oe terms in <i>x</i> or constant ter	ms collected

Question	Answer	Mark	Comme	ents	
	90÷5 or 18	M1			
-	2 × their 18 or 36	M1dep	M2 $\frac{2}{5} \times 90$		
-	180 – 90 – their 36	M1dep	oe eg 90 – their 36		
-	90		any order		
	36	A1			
	54				
	Ad				
	Beware of incorrect methods, eg divid	oy 5			
22	180 ÷ 5 = 36				
	180 ÷ 2 = 90			M0M0M0A0	
	180 - 90 - 36 = 54				
-	Answer 90, 36, 54				
	Beware of 18 coming from wrong wo	rking			
	90 ÷ 2 = 45				
	90 ÷ 5 = 18		M0M0M0A0		
	90 ÷ 7 =				
F	However, it is not incorrect to work with 180 ÷ 10				
	Trial and Improvement scores 0 or 4				

23 number of pets B1	
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Question	Answer	Mark	Comments
	Says that the wrong line has been given		eg the line should be $y = -1$
	or		
	says that for the given reflection the image would be in the second quadrant (may be implied by sketch)		eg the triangle would move to the other side of the <i>y</i> -axis
	or	B1	
	says that the given line is vertical		eg $x = -1$ is vertical
24(a)	or		
	gives the coordinates of at least		eg (1, 1) would move to (–3, 1)
	one image point under the given reflection		(1, 3) would move to (–3, 3)
	or		(4, 1) would move to (–6, 1)
	-		
	says that after the given reflection, a rotation 180° (centre $(-1, -1)$) or an enlargement, scale factor -1 (centre $(-1, -1)$) is needed		

	Additional Guidance	
	It is the wrong line/axis (of reflection)	B1
	It's not $x = -1$	B1
	The line should be horizontal	B1
	y = -1	B1
	x = -1 line drawn with explanation that it is incorrect	B1
	Q should be to the left of P	B1
	Correct line drawn, with indication that it should be that line	B1
	Correct statement with irrelevant statement	
	eg It's the wrong line and Q is in the wrong place	B1
	Correct line drawn, but no explanation or equation given	В0
24(a) cont	x = -1 line drawn with no explanation that it is incorrect	В0
	It should be reflected in the <i>y</i> -axis	В0
	It is not a reflection in $x = -1$	В0
	Should be rotation about $y = -1$	В0
	They are not an equal distance from each other	В0
	It should be the point $x = -1$	В0
	Q is in the wrong place	В0
	It is a reflection in the <i>x</i> -axis then a translation by $\begin{pmatrix} 0 \\ -2 \end{pmatrix}$	B0
	Correct statement with incorrect statement	B0
	eg It's the wrong line, it should be $x = -2$	
	If more than one image point is given, they must all be correct	

Question	Answer	Mark	Comme	ents
	Should say the centre of rotation (is <i>O</i>)	B1	oe statement accept 'axis of rotation'	or 'point'
	Ado	ditional G	uidance	
-	Allow origin or (0, 0) for <i>O</i>			
	Should be about <i>O</i>			B1
	There is no centre	B1		
	It should be around a point	B1		
24/h)	It doesn't give the coordinates	B1		
24(b)	Should/could be 270° clockwise about <i>O</i>			B1
	Should/could be 270° clockwise			В0
	Should be rotation through 90° clocky	vise abou	t <i>0</i>	B0
-	It is a reflection 90° anticlockwise with	n centre C)	B0
	It's not reflected on a point	B0		
	Doesn't say which line you're turning		В0	
	Correct statement with incorrect state	ment		
	eg It should give a centre of rotation a	at (0, 1)		В0

	64	B1	accept 4 ³	
25(a)	Ad			
20(0)	4 ³ and incorrect value given			
	eg 4 ³ = 32			B0

Question	Answer	Mark	Comme	nts
25(b)	-5 -13	B2	condone –13 –5 B1 –5 as first term or ft their first term – 8	
	$60 \times 4 \text{ or } 4(a \times 60) \text{ or } 4a \times 60$ or $\frac{b}{a} = 60 \text{ or } \frac{4b}{\frac{b}{60}}$ or $4b = 240a$ or $\frac{240a}{a}$	M1	accept any multiplication	ı signs
	240	A1	Condone $\frac{240}{1}$	
	Additional Guidance			
26	Correct answer found by substituting appropriate values for a and b			M1A1
	Incorrect answer found by substituting appropriate values for a and b			M0A0
	Award M1 for 60×4 or 240 in working, either as individual expressions or as part of longer expressions			
	eg $4 \times 60 = 240$, answer $240b$			M1A0
	eg $\frac{4 \times 60 \times a}{4b}$			M1A0
	Do not award M1 for 240 within a list beyond 240	of multiple	es of 60 that continues	

Question	Answer	Mark	Comme	nts
	(27 =) 3 ³	M1		
	$((3^2)^7 =) 3^{2 \times 7}$ or $((3^2)^7 =) 3^{14}$	M1		
	3 ¹⁷	A1ft	ft 3 ^{<i>a</i>} and 3 ^{<i>b</i>} then answer 3 ^{<i>a</i>+<i>b</i>} with M1M0 or M0M1 scored	
27	Additional Guidance			
	Answer 3 ¹⁷ with no incorrect working			M1M1A1
	3 ¹⁷ in working with 17 on the answer line or both 3 ¹⁷ and 17 on the answer line			M1M1A1
	$3^3 \times 3^9 = 3^{12}$			M1M0A1ft
	Evaluation of powers of 3 as values only			M0M0A0
	Answer 17 with no valid working			M0M0A0

Question	Answer	Mark	Comments	
	Alternative method 1: working in te	erms of π	I	
	π (×) 4 ² (×) 10 or 160π or [502, 503]	M1	oe accept 3 or better for π accept 480 or 496	
-	2/3 (×) π (×) 6 ³ or 144π or [452, 453]	M1	oe accept 3 or better for π accept 0.66 or 0.67 or better for $\frac{2}{3}$ accept 432 or 446(.4)	
	160π and 144π or [502, 503] and [452, 453]	A1	oe values accept 480 and 432 or 496 and 446(.4)	
28	160π and 144π and cylinder or [502, 503] and [452, 453] and cylinder or cylinder is 16π greater	A1ft	ft correct decision for their 160π and their 144π with M1M1 scored accept 480 and 432 and cylinder or 496 and 446(.4) and cylinder	
	Alternative method 2: working without π			
-	4 ² (×) 10 or 160	M1	ое	
	$\frac{2}{3}$ (×) 6 ³ or 144	M1	oe accept 0.66 or 0.67 or better for $\frac{2}{3}$	
-	160 and 144	A1	oe values	
	160 and 144 and cylinder	A1ft	ft correct decision for their 160 and their 144 with M1M1 scored	
-	Additional Guidance for this question is on the next page			

	Additional Guidance			
	Better than 3 for π could be 3.1, 3.14, 3.142 or $\frac{22}{7}$			
	160 π with incorrect method for hemisphere	M1M0A0A0		
	144 π with incorrect method for cylinder	M0M1A0A0		
	160π and 144π with incorrect decision or no decision	M1M1A1A0		
	160 and 144 with incorrect or no decision	M1M1A1A0		
28	Accept values given as fractions for the first A mark, but for the second A mark, they must have a common denominator.			
	eg 160 π and $\frac{432\pi}{3}$ and cylinder	M1M1A1A0		
	eg $\frac{480}{3}$ and $\frac{432}{3}$ and cylinder	M1M1A1A1		
	Working with π for one value but not the other can only score M1			
	eg 160 π and 144 (with or without a decision)	M1 only		
	Do not allow M1 for a correct formula as part of an incorrect formula			
	eg $\frac{1}{3} \times \pi \times 4^2 \times 10$	MO		

Question	Answer	Mark	Comments		
	Alternative method 1: total amount of each colour (judgement accepted that ratio is not 4 : 3)				
-	60 ÷ (2 + 1) or 20 or 40	M1			
	80 + their 20 or 100	M1dep			
-	28 + 2 × their 20 or 68	M1dep	dep on first M1 only		
	100 and 68 and No	A1			
-			nuch white should have been added or y or how much there should be now		
	60 ÷ (2 + 1) or 20 or 40	M1			
	80 + their 20 or 100	M1dep			
	their 100 \div 4 \times 3 or 75	M1dep	dep on M2		
-	(75 – 2 × 20 =) 35 and No or		comparing 35 to 28		
29	40 and (75 – 28 =) 47 and No or	A1			
	75 and 68 and No				
-	Alternative method 3: total of white and how much red should have been added or how much there should have been originally or how much there should be now				
	60 ÷ (2 + 1) or 20 or 40	M1			
	28 + 2 × their 20 or 68	M1dep			
	their 68 ÷ 3 × 4 or 90 $\frac{2}{3}$ or $\frac{272}{3}$	M1dep	dep on M2		
	$(90\frac{2}{3} - 20 =) 70\frac{2}{3}$ and No		comparing $70\frac{2}{3}$ to 80		
	or 20 and $(90\frac{2}{3} - 80 =) 10\frac{2}{3}$ and No	A1			
	or $90\frac{2}{3}$ and 100 and No				
	The scheme for question 29 continues on the next page				

Question	Answer	Mark	Comme	nts	
	Alternative method 4: total of red and what it should be for total amount of paint				
	60 ÷ (2 + 1) or 20 or 40	M1			
	80 + their 20 or 100	M1dep			
	(60 + 80 + 28) ÷ (4 + 3) × 4 or 96	M1			
	100 and 96 and No	A1			
	Alternative method 5: total of white	e and wha	at it should be for total ar	nount of paint	
	60 ÷ (2 + 1) or 20 or 40	M1			
	28 + 2 × their 20 or 68	M1dep			
20	(60 + 80 + 28) ÷ (4 + 3) × 3 or 72	M1			
29 cont	68 and 72 and No	A1			
	Additional Guidance				
	20 from 80 ÷ 4 is incorrect				
-	With no incorrect working, 'He should implies full marks	M1M1M1A1			
-	'No' can be implied, eg on alt 1 accer more white'	M1M1M1A1			
	Condone dubious notation eg 20:4	M1M1M1A1			
	Ignore further work if 100 and 68 and	M1M1M1A1			
	Only works out the amounts of red ar total amount of paint, eg, 168 \div 7 \times 4	M0M0M1A0			

Question	Answer	Mark	Comments	
30(a)	10^{5} or 25000 2.5×10^{4}	M1 A1	oe correct value not in standard fo eg 25 × 10^3	orm
	Additional Guidance			
	Condone 2.5 · 10 ⁴			A1
	Condone different spacing or commas eg 25000 or 250,00			A0

	c = 3 and $d = -2$	B2	B1 c = 3 or d = -2 or	
30(b)			$c = 10^3$ and/or $d = 10^{-2}$	
		Additional Guidance		
	One or both of the values may be embedded for B1 only			

	<i>V</i> is directly proportional to <i>H</i>		
31	\checkmark <i>V</i> is inversely proportional to <i>H</i>	B1	
	\checkmark <i>V</i> is directly proportional to $\frac{1}{H}$		
	<i>V</i> is inversely proportional to $\frac{1}{H}$		