## AQA

Please write clearly in block capitals.

Centre number


Candidate number


Surname $\qquad$
Forename(s)
Candidate signature
I declare this is my own work.

## GCSE

MATHEMATICS

## Higher Tier

Thursday 3 November 2022 Morning
Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).



## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper.

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $2-3$ |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| 24 |  |
| TOTAL |  | These must be tagged securely to this answer book.

## Advice

In all calculations, show clearly how you work out your answer.

1 Work out $\frac{4^{6}-11}{\sqrt{625}-225}$
Circle your answer.

$$
\begin{array}{llll}
-61.6 & -20.425 & 204.25 & 3870.56
\end{array}
$$

2 Work out $\left(3.1 \times 10^{9}\right)^{2}$
Circle your answer.
$6.2 \times 10^{18}$
$6.2 \times 10^{81}$
$9.61 \times 10^{18}$
$9.61 \times 10^{81}$

3 The equation of a line is $y=3 x-6$
Circle the coordinates of the $y$-intercept.
(0, -6)
$(-6,0)$
(0, 3)
$(3,0)$
$4 \quad a \times b^{4}=c$
Circle the correct expression for $a$.
$\frac{c}{\sqrt[4]{b}} \quad \frac{c}{b^{-4}} \quad\left(\frac{c}{b}\right)^{4} \quad \frac{c}{b^{4}}$

5 Written as the product of prime factors,

$$
12600=2^{3} \times 3^{2} \times 5^{2} \times 7
$$

and
$14112=2^{5} \times 3^{2} \times 7^{2}$
Work out the highest common factor (HCF) of 12600 and 14112
Give your answer as an integer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

6 The composite bar chart shows information about the percentage of drinks sold by a café in 2007 and 2019


6 (a) In 2007 the café sold a total of 24000 drinks.
How many more teas than coffees were sold?
[2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

6 (b) Were more coffees sold at the café in 2019 than in 2007?
Tick a box.


Give a reason for your answer.
$\qquad$
$\qquad$
$\qquad$

7 (a) $k$ is a whole number between 40 and 50
The cube root of $k$ is 3 , to the nearest whole number.
Work out the largest possible value of $k$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

7 (b) Fay tries to solve $x^{2}=100$
She says,
"The only possible value of $x$ is 10 "
Give a reason why she is not correct.
[1 mark]
$\qquad$
$\qquad$
The cube root of $k$ is 3 , to the nearest whole number.
[2 marks]

8 (a) Here is a cuboid.
$w, x$ and $y$ are different whole numbers.


The total length of all the edges of the cuboid is 80 cm
The volume is greater than $200 \mathrm{~cm}^{3}$
Work out one possible set of values for $w, x$ and $y$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$w=$ $x=$ $y=$

8 (b) Here is a solid cube.


Circle the expression for the total surface area in $\mathrm{cm}^{2}$
$36 a^{2}$
$54 a^{2}$

9 The 47th triangular number is 1128
The 48th triangular number is 1176
Work out the 49th triangular number.
$\qquad$
$\qquad$

Answer $\qquad$

10 The $n$th terms of two linear sequences, $A$ and $B$, are added to give the $n$th term of a new sequence.

The new sequence starts

$$
\begin{array}{llll}
8 & 13 & 18 & 23
\end{array}
$$

The $n$th term of sequence A is $n+1$
Work out the $n$th term of sequence B.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

11 A tank contains 40 litres of water.

11 (a) Water leaks out of the tank at a rate of 1.2 litres per minute.
The leak is stopped after 20 minutes.
Show that, when the leak is stopped, the tank contains 16 litres of water.
[1 mark]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

11 (b) The tank is refilled with water from a tap.
The graph shows the amount of water in the tank after the leak is stopped.


Complete this report by writing a number in each answer space.

## Report

$\qquad$ minutes after the leak is stopped, the tap starts to refill the tank.

The rate at which the tank refills is $\qquad$ litres per minute.
$\qquad$
$\qquad$
$\qquad$
$\qquad$


12 The length of this rectangle is 6 times the width.


Not drawn accurately

Two of these rectangles are joined, with no overlap, to make this L-shape.


The perimeter of the L-shape is 98.8 cm
Work out the value of the perimeter of one of the rectangles.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer cm
13 Trapezium DEFG is formed by joining
triangle DEH
to
rectangle EFGH.

$A B C$ is similar to $D E H$.
Work out the area of $D E F G$.

Not drawn accurately
[5 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer $\qquad$ $\mathrm{cm}^{2}$

14 Fred bought an apartment for $£ 137500$
He made 8\% profit when he sold the apartment.
He used all of this profit to pay $40 \%$ of the deposit on a house.
The deposit was one sixth of the price of the house.
Work out the price of the house.
[4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £ $\qquad$

15 Circle the correct statement.
[1 mark]

$$
1 \mathrm{~m}^{2}=100 \mathrm{~mm}^{2} \quad 1 \mathrm{~cm}^{2}=100 \mathrm{~mm}^{2} \quad 1 \mathrm{~m}^{2}=100 \mathrm{~cm}^{2} \quad 1 \mathrm{~km}^{2}=100 \mathrm{~m}^{2}
$$

16 Here is a sketch of a graph.


Circle the possible equation of the graph.

$$
y=x^{2}+1 \quad y=\frac{1}{x}+1 \quad y=x^{3}+1 \quad y=1-x^{2}
$$

17 A sequence of numbers is formed by the iterative process

$$
u_{n+1}=\frac{20}{u_{n}+3} \quad \text { where } \quad u_{1}=1
$$

Work out $u_{3}$
Circle your answer.
$\frac{40}{11}$
$\frac{5}{2}$
7
5


Here are the points the team scored in the 19 away games.
85
$89 \quad 93$
95
96
$96 \quad 98$
98
98
99
100
103
105 107 109 110 114 119 126

18 (a) On the grid, draw a box plot for the away games.


Use one statistical measure to support your decision.

18 (c) Was the number of points scored more consistent in home games or away games? Use one statistical measure to support your decision.
$\qquad$

19 Using the quadratic formula, or otherwise, solve $3 x^{2}+x-5=0$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

20 A vending machine has a different item in each section.
It sells
7 drinks, 3 of which are juice
5 snacks, 2 of which are fruit bars
11 meals, 4 of which are salad.
One drink, one snack and one meal are chosen at random.
Show that the probability of getting a juice, a fruit bar and a salad is more than $5 \%$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
$21 \quad \mathrm{f}(x)=\frac{3 x+9}{5} \quad$ and $\quad \mathrm{g}(x)=6 x-1$

21 (a) Show that $\mathrm{gf}(2)$ is an integer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

21 (b) Show that $\mathrm{f}^{-1}(8)$ is not an integer.
$\qquad$
$\qquad$
$\qquad$
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$\qquad$


23 (a) Work out an estimate of the mean time the 61 students spent revising.
You may use the table to help you.

| Time, $\boldsymbol{x}$ (hours) | Frequency | Midpoint |  |
| :---: | :---: | :---: | :---: |
| $0 \leqslant x<6$ |  |  |  |
| $6 \leqslant x<10$ |  |  |  |
| $10 \leqslant x<12$ |  |  |  |
| $12 \leqslant x<16$ |  |  |  |
| $16 \leqslant x<20$ |  |  |  |

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ hours

23 (b) Give a reason why the answer to part (a) is an estimate.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$24 \quad B$ is 60 miles from $A$ on a bearing of $170^{\circ}$


A ship sails from $A$ on a bearing of $247^{\circ}$
It travels at a constant speed of 23 mph for $1 \frac{1}{2}$ hours.
Is the ship now closer to $B$ than it was when it left $A$ ?
You must show your working.
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
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$\qquad$
$\qquad$
$\qquad$

Two congruent parallelograms, $P Q R V$ and $V R S T$, are joined.

$\overrightarrow{Q P}=\mathbf{a} \quad \overrightarrow{P V}=\mathbf{b}$
$X$ is the midpoint of $V T$.
$V W: W R=1: 2$
Prove that $Q, W$ and $X$ lie on a straight line.
$\qquad$
$\qquad$
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$\qquad$

26 Helena ran an 800-metre race in 140 seconds.
The speed-time graph represents the first 100 seconds of her run.


Helena ran the last 40 seconds with constant deceleration.
Work out her speed as she finished the race.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ metres per second

27 In a class there are
$n$ boys
a total of 25 students.
Two of the students are chosen at random.
The probability that both students are boys is $\frac{7}{20}$
Work out the value of $n$.
[4 marks]
$\qquad$
$\qquad$
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$\qquad$
$\qquad$
$n=$ $\qquad$
$28 \quad A B C D E F$ is a triangular prism.
$P$ is a point on $E F$.

$E B=29 \mathrm{~cm}$
Angle $E B P=35^{\circ}$
Angle $E P B=114^{\circ}$
Work out the length of $E P$.
$\qquad$





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